

Davisson-Germer Experiment



Photons:

$$E_{ph} = h\nu$$

$$p = \hbar k = h/\lambda$$

Wave \rightarrow Particle

What about the opposite?

Particle \rightarrow Wave ?

$$\lambda = h/p$$



Matter waves:

$$\lambda_B = \frac{h}{p} = \frac{h}{mv} = \frac{h}{\sqrt{2mK}}$$

Wavelength for a walking man?

Wavelength for a moving electron?

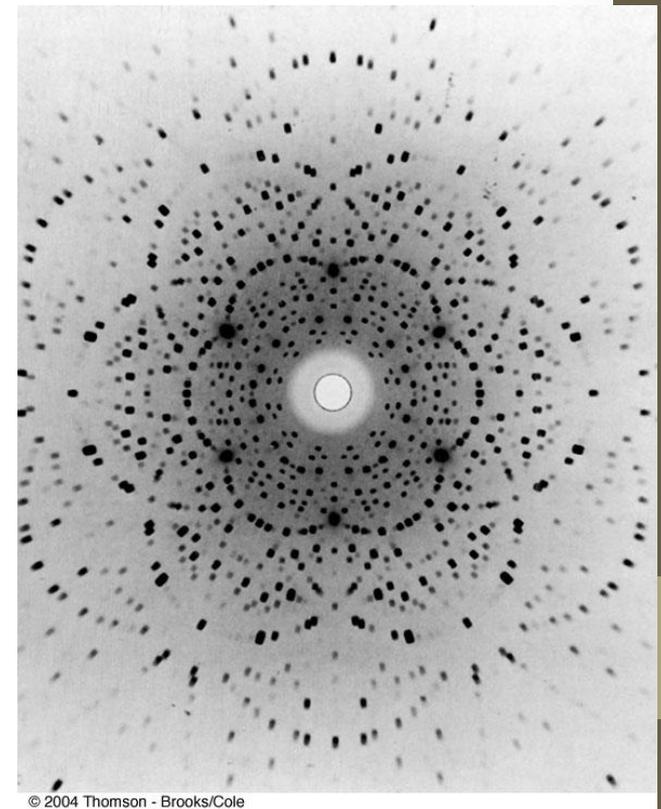
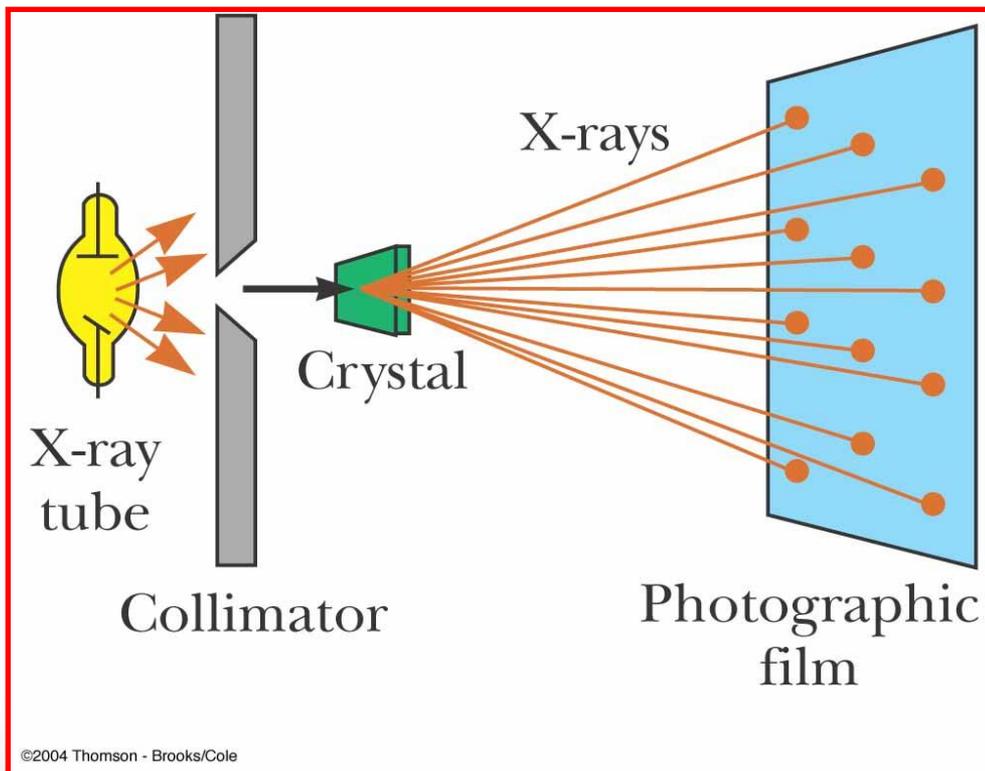
What is the wavelengths difference for 5 eV electron and 5 eV photon?

How to reveal the wave properties of electrons?



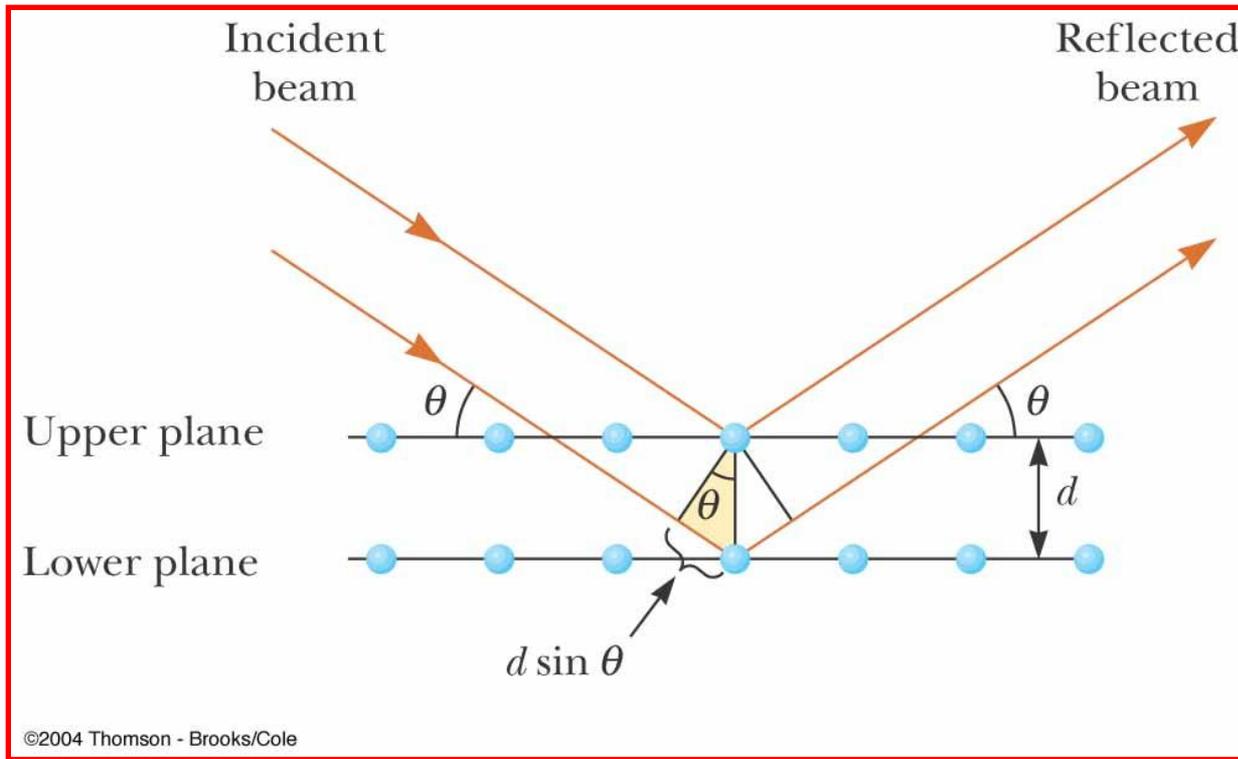
X-rays diffraction:

X-rays are electromagnetic waves with
 $\lambda = 10^{-8}$ to 10^{-12} $m = 10 - 0.001$ nm





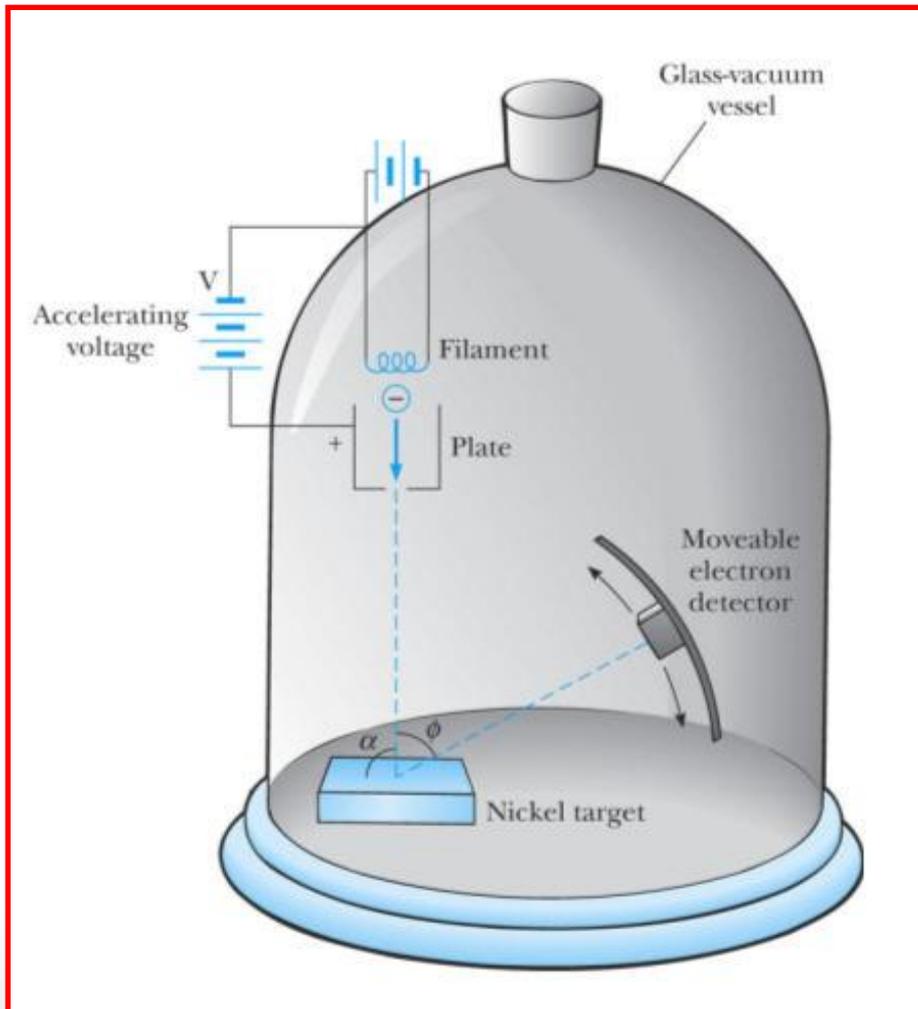
Bragg's law:



$$2d \sin \theta = n\lambda$$

If θ and λ are known,
 d can be determined

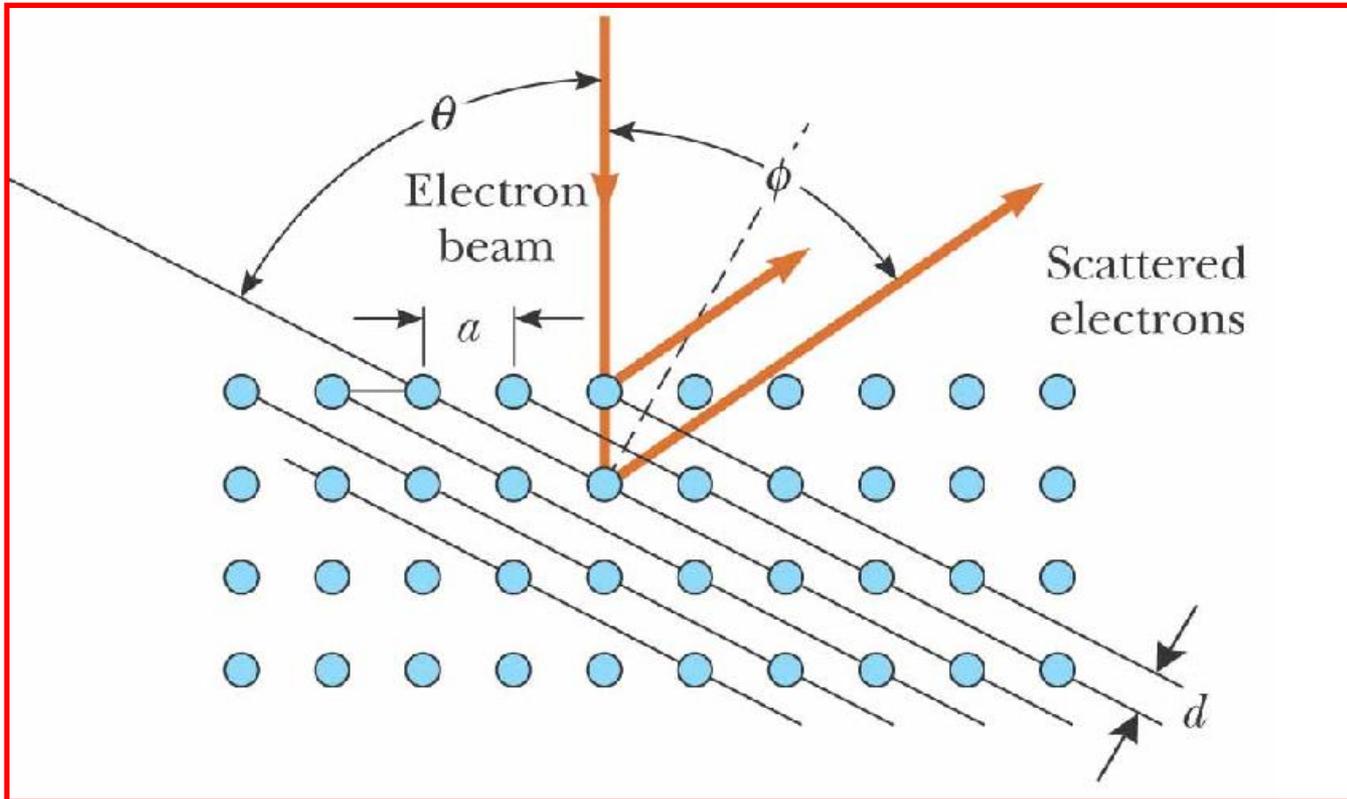
Davisson-Germer experiment:



- Electrons were directed onto nickel crystals
- Accelerating voltage is used to control electron energy: $E = |e|V$
- The scattering angle and intensity (electron current) are detected
 - φ is the scattering angle



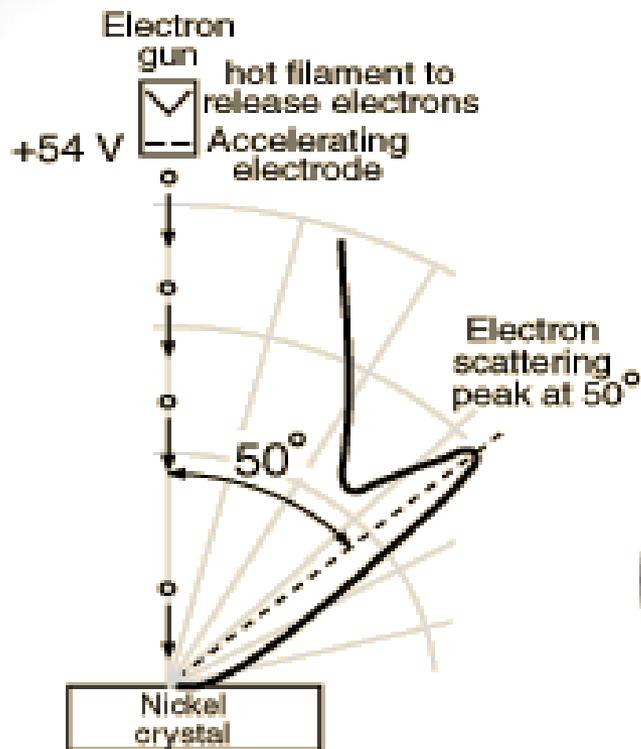
Electron scattering:



From X-ray experiments:
 $d = 0.091 \text{ nm}$

$$2d \sin \theta = n\lambda$$

For $\phi = 50^\circ$
($\theta = 65^\circ$):
 $\lambda = 0.165 \text{ nm}$



Theory

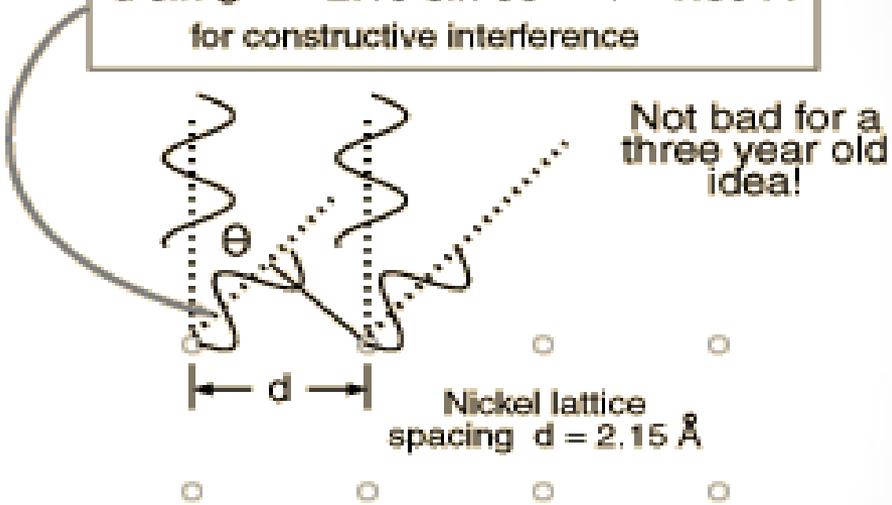
$$\lambda = \frac{h}{mv} = 1.67 \text{ \AA} \text{ for } 54 \text{ V}$$

Experiment

Pathlength difference

$$d \sin \theta = 2.15 \sin 50^\circ = \lambda = 1.65 \text{ \AA}$$

for constructive interference



1924
de Broglie's hypothesis

1927
Davisson-Germer experiment

1929
Nobel Prize for de Broglie

- Application of diffraction to measure atomic spacing
- Single crystal Ni target
- Proved deBroglie hypothesis that $\lambda=h/p$

Davisson-Germer experiment

Proof that $\lambda=h/p$

Accelerated electrons have energy eV:

$$eV = \frac{1}{2} mv^2 \Rightarrow v = (2Ve/m)^{1/2}$$

de Broglie said:

$$\lambda = h/p = h/(mv) = h/(2mVe)^{1/2} = 1.67 \text{ \AA}$$

Davisson-Germer found lattice spacing:

$$\lambda = d \sin \theta = 1.65 \text{ \AA}$$

Excellent agreement between theory and experiment!

Application: Pressure sensing

- Atomic spacing changes with pressure:

$$\text{Pressure} = E(\Delta L/L)$$

Where E = Young's modulus (N/m^2)

- As d (spacing between atomic planes) changes, the angle of diffraction changes
- Diffraction rings move apart or closer together